

## Binary Counting

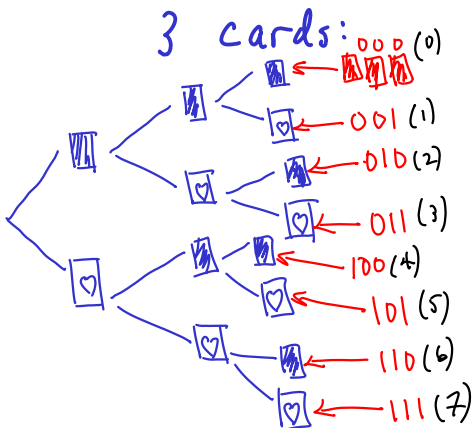
### I. Counting with Two Cards

Your team has been issued 2 playing cards. Line the cards up in a row and come up with a system for representing the numbers 0 through 3. Complete column (a) below. A face-up card is left blank and a face-down card is shaded in.

Number	(a) Team's agreed-upon arrangement	(b) Class' agreed-upon arrangement	(c) Using 0s and 1s
0			<u>0</u> <u>0</u>
1			<u>0</u> <u>1</u>
2			<u>1</u> <u>0</u>
3			<u>1</u> <u>1</u>

### II. Counting with 1, 2, 3, 4, and More Cards

Your team will now be given two additional cards, for a total of four. In the last exercise, we were able to represent 4 different values – 0, 1, 2, 3 – using two cards. How many values can you represent using different numbers of cards?



Number of Cards	Number of Values
1 card	$2^1$
2 cards	$2^2$
3 cards	$2^3$
4 cards	
5 cards	$3^2$
20 cards	$2^{20} = 1,048,576$
$n$ cards	$2^n$

Handwritten notes on the table:

- Red arrow: 2 ← 0, 1
- Green arrow: 4 ← 0, 1, 2, 3
- Black arrow: 8 ← 0, 1, ..., 7

### III. Binary Counting with 4 bits

Using face-up and face-down cards is a hands-on way to represent zeros and ones known as **BINARY DIGITS**, or **bits** for short. Using just zeros and ones, we can come up with a way to represent the base-10 (decimal) numbers you've always used.

Let's complete this together:

Decimal #	Binary #		Decimal #	Binary #
0	0 0 0 0	$\begin{matrix} 19 \\ 20 \\ 21 \\ \vdots \\ 99 \\ 100 \end{matrix}$	8	1 0 0 0
1	0 0 0 1		9	1 0 0 1
2	0 0 1 0		10	1 0 1 0
3	0 0 1 1		11	1 0 1 1
4	0 1 0 0		12	1 1 0 0
5	0 1 0 1		13	1 1 0 1
6	0 1 1 0		14	1 1 1 0
7	0 1 1 1		15	1 1 1 1

$\begin{matrix} 8 \\ 1 \\ 0 \\ 0 \\ 0 \end{matrix}$

### IV. HW: Count from 0 to 31 in Binary.

Decimal #	Binary #	Decimal #	Binary #
0	0 0 0 0 0		
1	- - - - -		
2			
3			
4			